

電機機械

Date . . .

§Ch1. 變壓器

① 等效電路 $\left[\begin{array}{l} \text{一、二側轉換} \\ \text{二、} \pi \text{ 連接} \end{array} \right.$

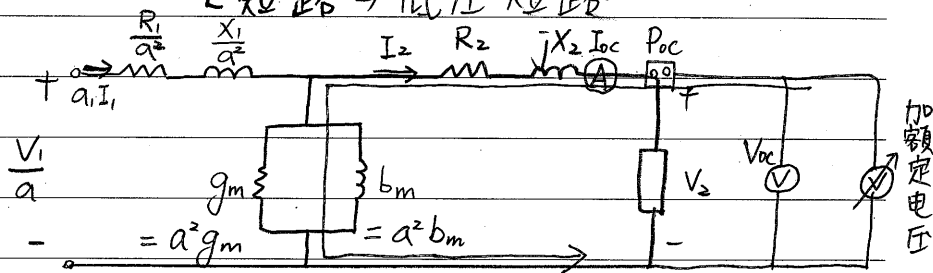
② 標么值 $\rightarrow$ 單相

③ 電壓分接頭 (一次側分接頭)
(調整二次側電壓)

$$a_1 = \frac{V_1}{V_2} = \frac{N_1}{N_2}$$

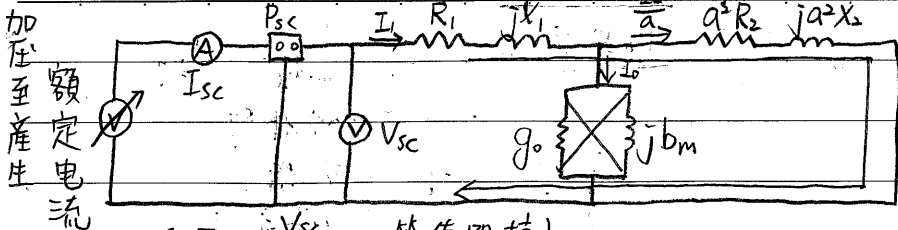
$$\Rightarrow \frac{N_1}{N_1'} = \frac{V_2'}{V_2}$$

④ 試驗 $\left[\begin{array}{l} \text{開路} \Rightarrow \text{高壓開路} \\ \text{短路} \Rightarrow \text{低壓短路} \end{array} \right.$



$$\left\{ \begin{array}{l} Y_0 = \frac{I_{oc}}{V_{oc}} \quad (\text{激磁導納}) \\ G_0 = \frac{P_{oc}}{V_{oc}^2} \quad (\text{電導}) \\ B_0 = \sqrt{Y_0^2 - G_0^2} \quad (\text{電納}) \end{array} \right.$$

Date



$$\begin{cases} Z_{SE} = \frac{V_{sc}}{I_{sc}} & (\text{等值阻抗}) \\ R_{eq} = \frac{P_{sc}}{I_{sc}^2} & (\text{电阻}) \\ X_{eq} = \sqrt{Z_{SE}^2 - R_{eq}^2} & (\text{电抗}) \end{cases}$$

⑤ 电压調整率 (VR%) $\Rightarrow VR\% = P \cos \theta \pm q \sin \theta$,

$$P = \frac{I_s \times R_{eq}}{V_2}, \quad q = \frac{I_s \times X_{eq}}{V_2}$$

$$\begin{cases} VR\%(\max) = \sqrt{P^2 + q^2}, & \cos \theta = \frac{P}{\sqrt{P^2 + q^2}} \\ VR\%(\min) = 0, & \cos \theta = \frac{q}{\sqrt{P^2 + q^2}} \end{cases}$$

⑥ 損失, 效率

銅損
鐵損

最大效率時負載 ($\frac{1}{m}$)

全日效率

$\rightarrow$ 鐵損 = 銅損

$$P_c = \left(\frac{1}{m}\right)^2 P_{c\text{滿}} \Rightarrow \frac{1}{m} = \sqrt{\frac{P_c}{P_{c\text{滿}}}}$$

⑦ 並聯 ⇒ 电压相同

1.) 條件 [單相 ⇒
三相]

一、二側額定电压相同
極性相同
匝數相同
阻抗內角相同 ⇒ 电流槽

$$\text{代数和 } I_1 = \frac{V}{Z_1} = \frac{V \angle 0^\circ}{Z_1 \angle \theta_1}$$

$$I_L = I_1 + I_2 + I_3$$

相序相同
相序角相同

2.) 計算: [阻抗. 實際值 (Z) ⇒ 求电流. 容量
阻抗. 標么值 (Z_{pu}) (I) (S)

$$I_1 = I_L \times \frac{Y_1 \times (S_{pu1})}{Y_1 + Y_2 + Y_3}$$

(S₁) (S_L) × S_{pu1} × S_{pu2} × S_{pu3}

⑧ 三相連接

[Y: 特性
Δ:]

Y-Y
Δ-Δ
Y-Δ
Δ-Y

★ [V-V] ⇒ $S_{V-V} = \sqrt{3} V_p I_p = \sqrt{3} V_L I_L$

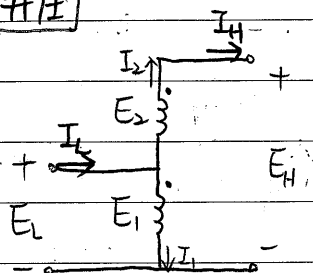
[U-V] [V_p = V_L
I_p = I_L]

$$\ast \quad \frac{S_w}{S} = \frac{\sqrt{3}}{2} V_p I_p = 0.866 V_p I_p$$

$$\frac{S_{V-V}}{S_{\Delta-V}} = \frac{\sqrt{3} V_p I_p}{3 V_p I_p} = \frac{\sqrt{3}}{3} = \frac{1}{\sqrt{3}} = 0.577$$

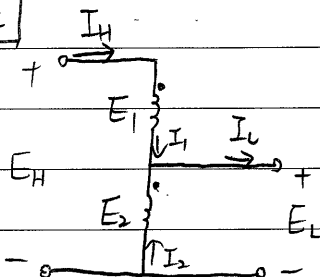
⑨ 自耦 T.L. (單相)

升压



$$S_{自} = S_{原} \left(1 + \frac{\text{共同电压}}{\text{非共同电压}} \right)$$

降压



一樣

⑩ 比压器 (P.T.)

→ 降压 T.L. (二次側 110V)

→ 二次側電流上升 ⇒ 不可短路

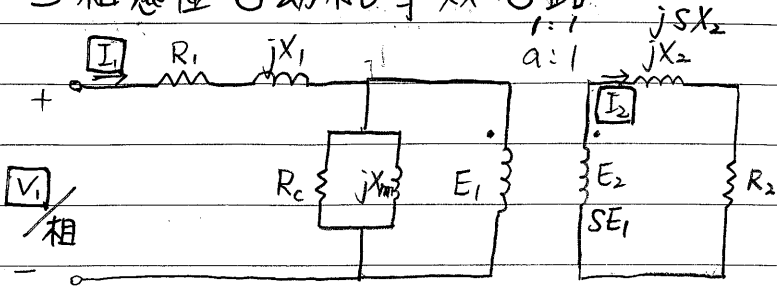
比流器 (C.T.)

→ 降電流 T.L. (二次側 5A)

→ 二次側電壓上升 ⇒ 不可開路

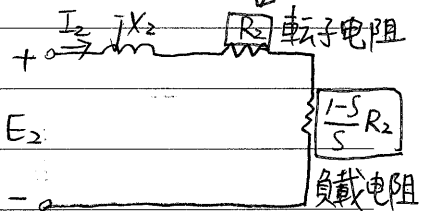
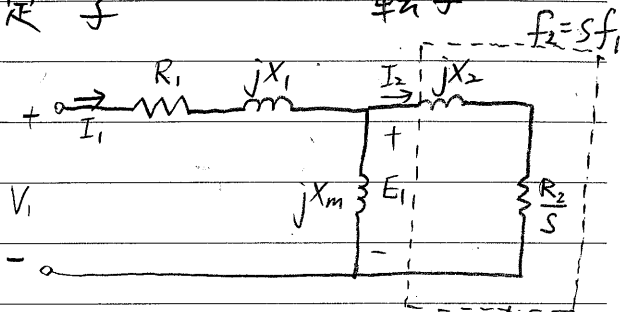
§ Ch 2. 感應機

① 三相感應电动机等效电路



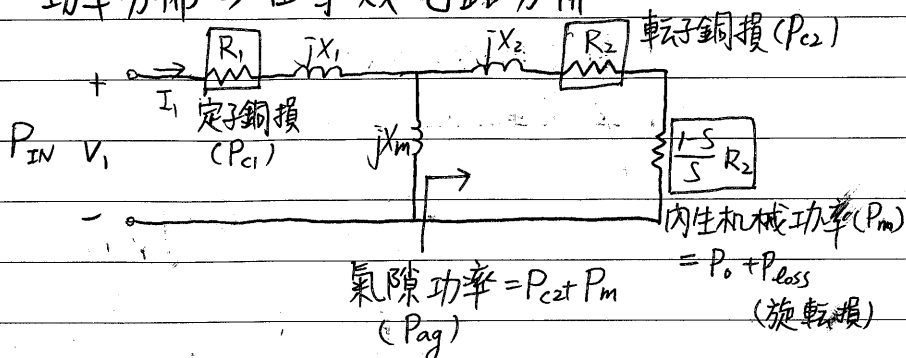
定子

轉子

$$\begin{cases} a=1 \\ R_c \text{ 忽略} \end{cases}$$


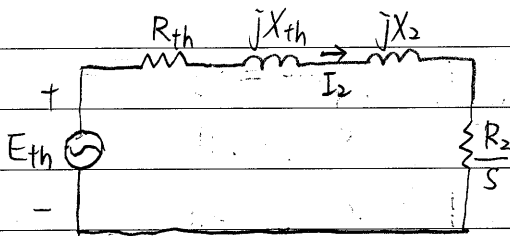
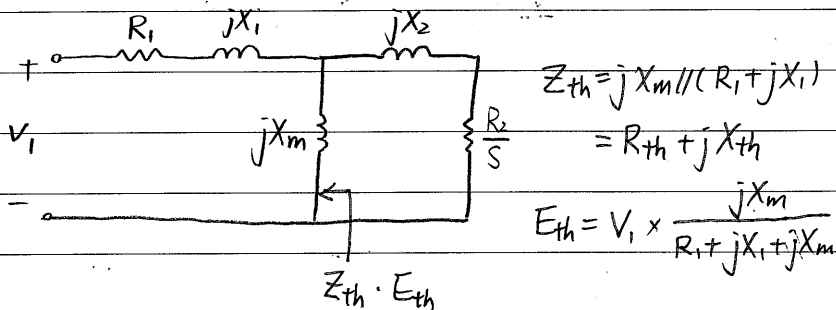
$$\frac{R_2}{s} = R_2 + \frac{1-s}{s} R_2$$

功率分佈 $\Rightarrow$ 由等效电路分析



$$* P_{ag} : P_{C2} : P_m = 1 : S : (1-S)$$

轉換 $\Rightarrow$ 定子側看入, 求戴維寧



② 轉矩

起動轉矩

最大轉矩之轉差率

最大轉矩 T_{max}

$$\left[\begin{array}{l} T = \frac{P_{ag}}{\omega_s} \quad 3 \times I_2^2 \times \frac{R_2}{s} = P_{ag}, \quad I_2 = \frac{E_{th}}{\sqrt{(R_{th} + \frac{R_2}{s})^2 + (X_{th} + X_2)^2}} \\ T_o = \frac{P_o}{\omega_r} \end{array} \right. \quad T = \frac{P_{ag}}{\omega_s} = \frac{P}{4\pi f} \times \frac{3 \times E_{th}^2}{(R_{th} + \frac{R_2}{s})^2 + (X_{th} + X_2)^2} \times \frac{R_2}{s}$$

$$\omega_s = \frac{2\pi}{60} N_s = \frac{2\pi}{60} \times \frac{120f}{p} = \frac{4\pi f}{p}$$

$$① T_s(s=1) = \frac{P}{4\pi f} \times \frac{3 E_{th}^2 R_2}{(R_{th} + R_2)^2 + (X_{th} + X_2)^2}$$

$$② \frac{R_2}{s} = \sqrt{R_{th}^2 + (X_{th} + X_2)^2}$$

$$\Rightarrow S_{max, T} = \frac{R_2}{\sqrt{R_{th}^2 + (X_{th} + X_2)^2}} \quad \times$$

③ 啟動

種類

鼠籠式 $\Rightarrow$ 降低電壓繞線式 $\Rightarrow$ 串接轉子電阻

條件

降低啟動電流, ($I_s \downarrow$)

(目的)

增加啟動轉矩, ($T_s \uparrow$)

$$\downarrow I_2 = \frac{E_{th} \downarrow}{\sqrt{(R_{th} + \frac{R_2}{s})^2 + (X_{th} + X_2)^2}}$$

- 降低电压 (鼠籠式) $\left\{ \begin{array}{l} \textcircled{1} Y-\Delta \\ \textcircled{2} \text{一次側串接电阻 (电抗)} \\ \textcircled{3} \text{自耦 } T_r \end{array} \right.$

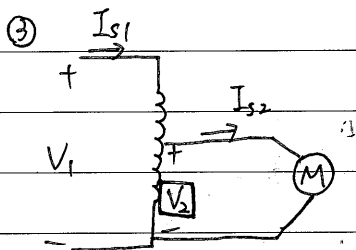
① $Y-\Delta$

$$* \left[\begin{array}{l} \frac{I_s(Y)}{I_s(\Delta)} = \frac{1}{3} \\ \frac{T_s(Y)}{T_s(\Delta)} = \frac{1}{3} \end{array} \right.$$

② $\left[\begin{array}{l} \text{电源电压 } (V_1) \\ \text{电动机电压 } (V_2) \end{array} \right. \quad \therefore \frac{V_2}{V_1} = \frac{1}{a}$

$$I_s = \frac{1}{a} I_s(\text{全})$$

$$T_s = \left(\frac{1}{a}\right)^2 T_s(\text{全})$$



$I_{s1} \Rightarrow$ 电源側电流

$I_{s2} \Rightarrow$ 电动机側电流

$$a = \frac{V_1}{V_2}$$

$$* \left[\begin{array}{l} V_2 \text{ 為 } \frac{1}{a} \text{ 倍 全电压} \\ \Rightarrow I_{s1} = \left(\frac{1}{a}\right)^2 I_s(\text{全}) \\ V_2 \text{ 為 全电压 時} \\ \Rightarrow I_{s1} = \frac{1}{a} I_s(\text{全}) \end{array} \right.$$

$$T_s = \left(\frac{1}{a}\right)^2 T_s(\text{全})$$

• 串接轉子電阻
(繞線式)

$$* \frac{R_2}{S_1} = \frac{R_2 + \boxed{R_s}}{S_2} \Rightarrow R_2 \uparrow \rightarrow S \uparrow \rightarrow n \downarrow \text{轉速控制}$$

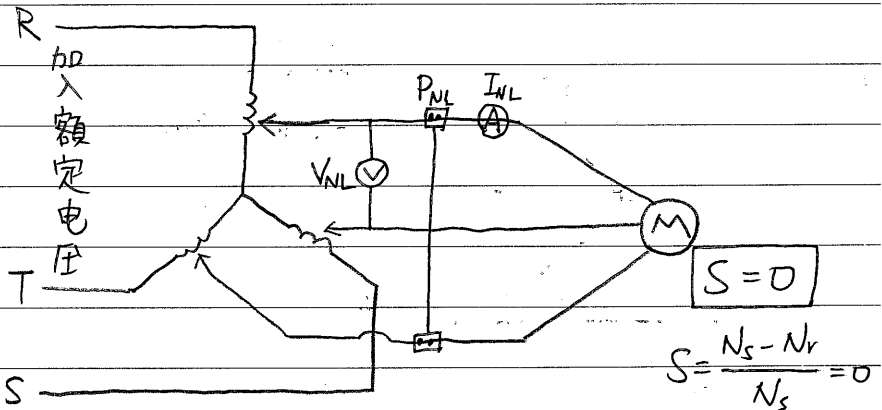
$$T = \frac{P}{4\pi f} \times 3 I_2^2 \times \boxed{\frac{R_2}{S}}$$

(定值)

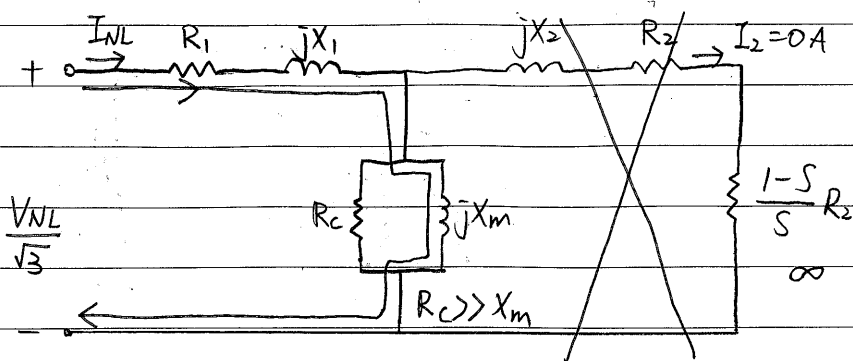
④ 試驗

無載 $\Rightarrow$ $\begin{cases} \text{求旋轉損} \\ \text{求磁化電感} \end{cases}$
 堵住轉子 $\Rightarrow$ $\begin{cases} \text{定子阻抗} \\ \text{轉子阻抗} \end{cases}$

• 無載接線圖：

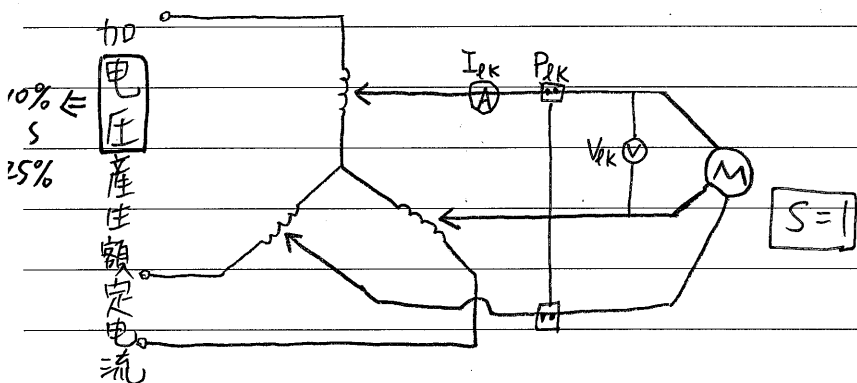


電路圖:

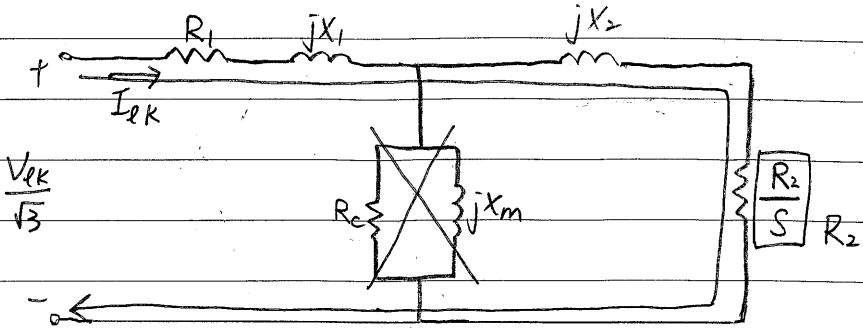


$$\left[\begin{aligned} \frac{\frac{V_{NL}}{3}}{I_{NL}} &= R_{NL} + jX_{NL} = R_{NL} + j(X_1 + X_m) \\ R_{NL} &= \frac{P_{NL}}{3 \times I_{NL}^2}, \quad P_{loss} = P_{IN} - 3(I_{NL})^2 R_1 \quad (\text{旋轉損}) \end{aligned} \right.$$

• 堵住轉子接綫圖:



電路圖:



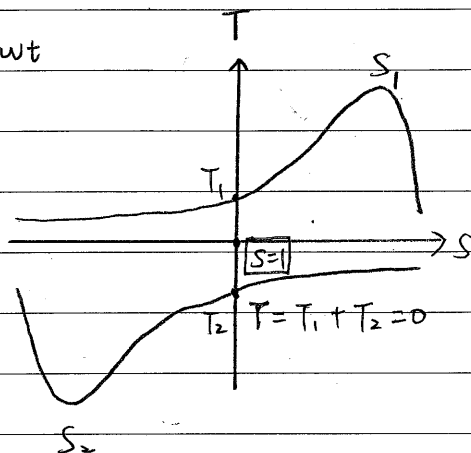
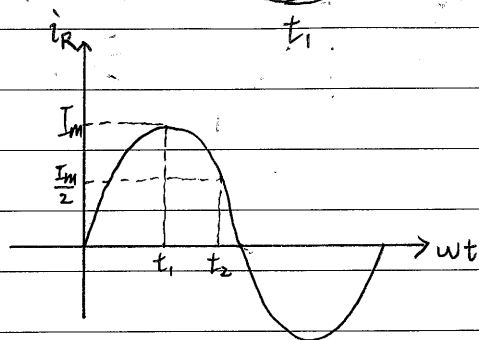
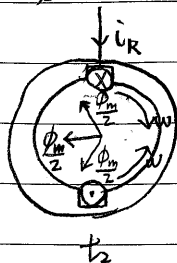
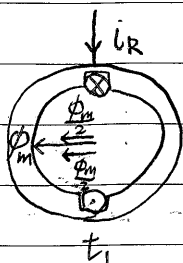
$$\frac{\frac{V_{pk}}{\sqrt{3}}}{I_{pk}} = (R_1 + R_2) + j(X_1 + X_2) \Rightarrow Z_{pk}$$

$$R_1 + R_2 = \frac{P_{pk}}{3(I_{pk})^2}$$

$$\boxed{X_1 + X_2} = \sqrt{Z_{pk}^2 - (R_1 + R_2)^2}$$

與頻率成正比

⑤ 單相感應電動機 $\Rightarrow$ 無法自行啟動 (雙旋轉磁場理論)



* 幫助啟動 $\Rightarrow$ 產生兩次旋轉磁場

啟動電容式

分相式 $\Rightarrow$ 兩繞阻相差 90° 電機角

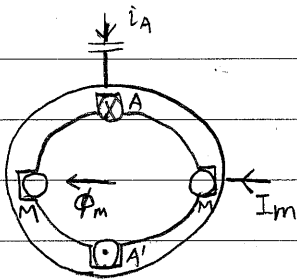
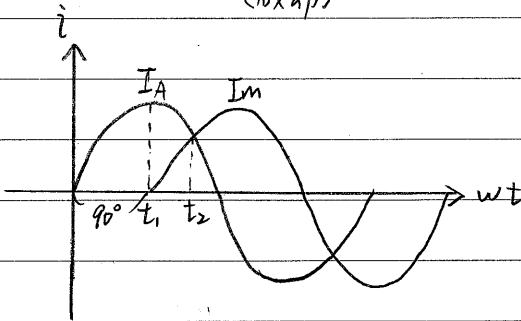
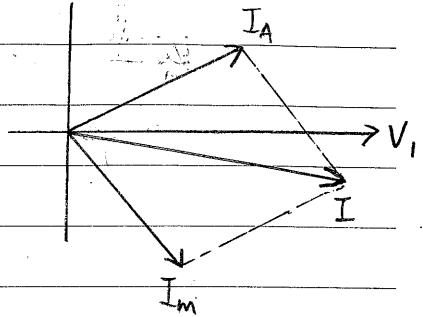
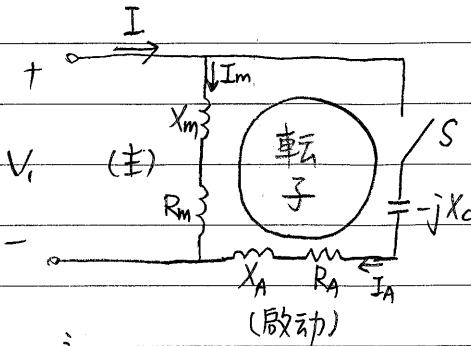
蔽極式

Date

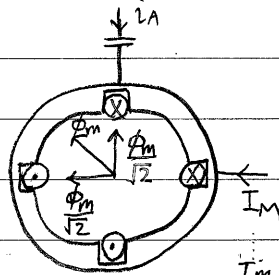
(I_A)

(I_m)

a. 启动电容式 (启动电流与主绕组电流相差 90° 电机角)



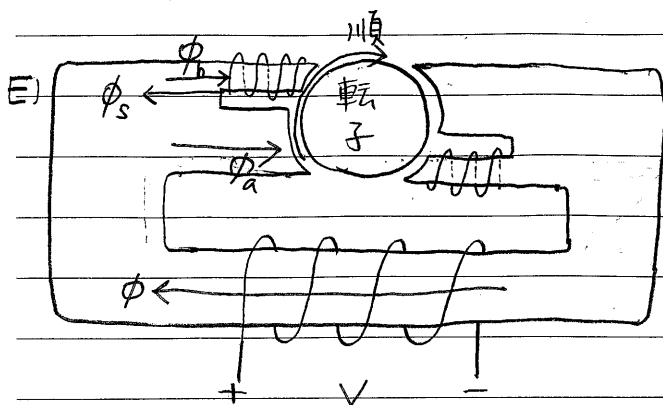
$$t=1 \begin{cases} I_A = I_m \\ I_m = 0 \end{cases}$$



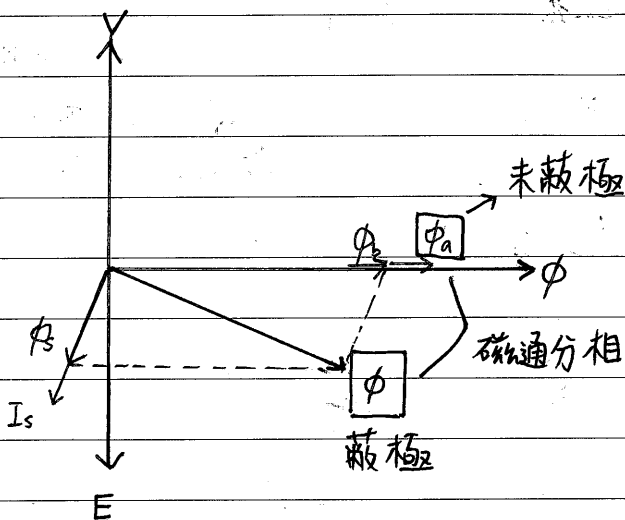
$$t=2 \begin{cases} I_A = \frac{I_m}{\sqrt{2}} \\ I_m = \frac{I_m}{\sqrt{2}} \end{cases}$$

※
$$X_C = X_A + \frac{R_m R_A}{X_m}$$

C. 蔽極式 $\Rightarrow$ 短路線圈



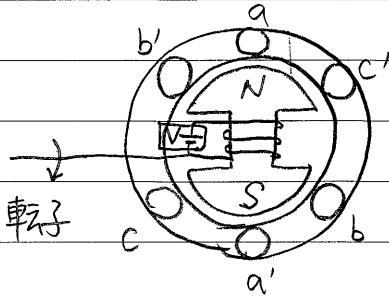
$$\phi = \phi_a + \phi_b$$



$$E = N \frac{\Delta \phi}{\Delta t} \quad \begin{matrix} \phi \angle 0^\circ \\ E \angle 90^\circ \end{matrix}$$

§ Ch3. 同步發電機

① 原理

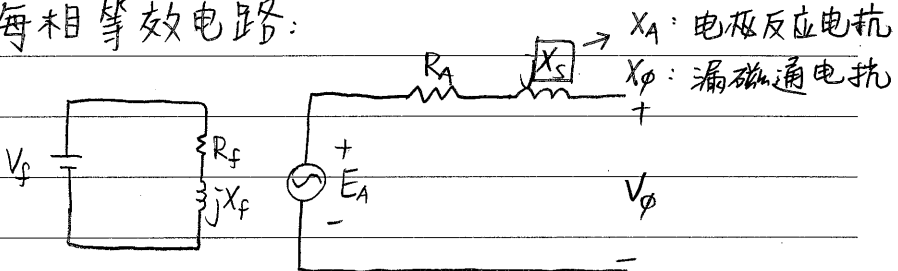


定子(三相繞組)

圓柱 $\Rightarrow$ 高速 $\Rightarrow$ 汽輪
 凸極 $\Rightarrow$ 低速 $\Rightarrow$ 水輪

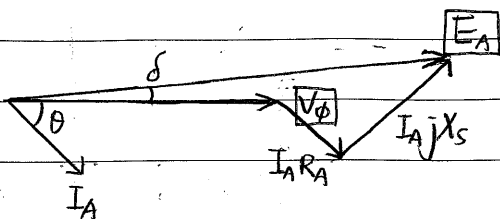
同步電抗

每相等效電路:

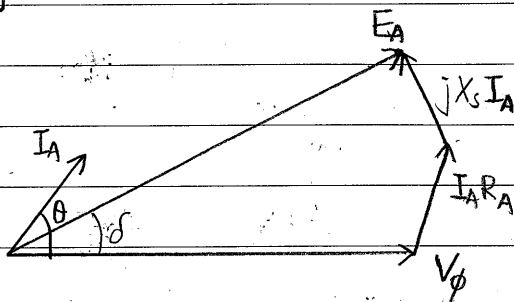


② 向量

落後:

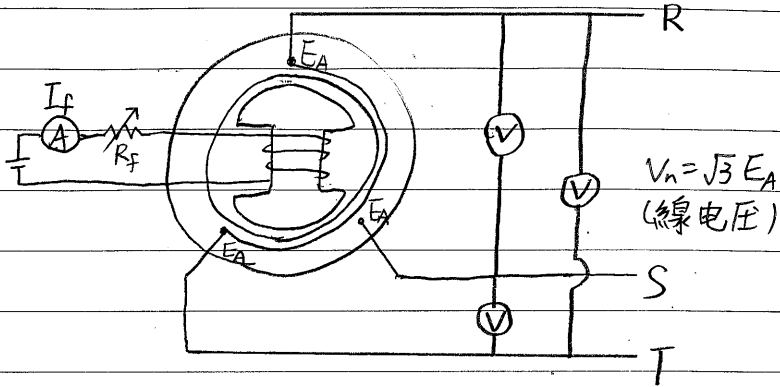


超前

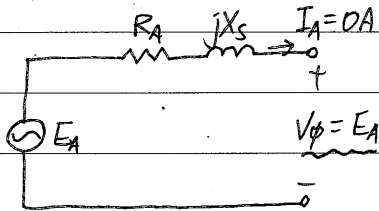


③ 試驗

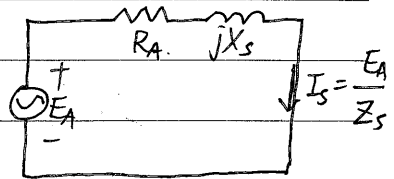
開路 $\Rightarrow$ 無載
短路



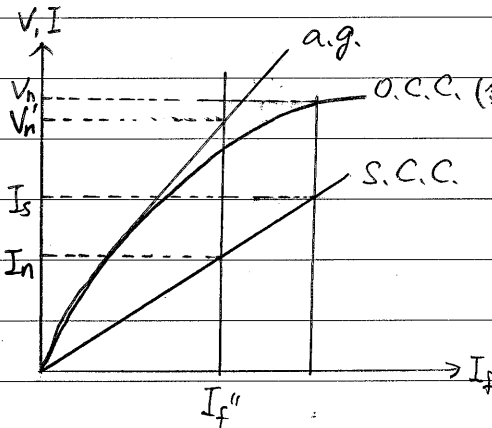
開路:



短路:



$$\therefore Z_s = \frac{E_a}{I_s} = \frac{V_\phi}{I_s}$$

相同 I_f 下

$$Z_s (\text{飽和}) = \frac{V_n / \sqrt{3}}{I_s}$$

$$Z_s (\text{未飽和}) = \frac{V_n' / \sqrt{3}}{I_n}$$

短路比 (SCR)

開路電壓在 **額定** 下的場電流

短路電流在 **額定** 下的場電流

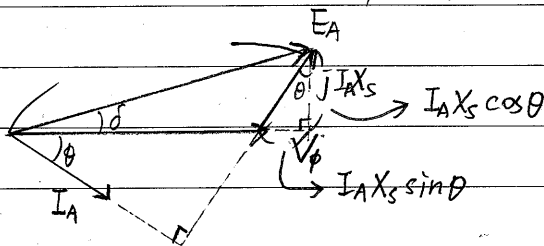
$$= \frac{I_f'}{I_f''} = \frac{I_s}{I_n} = \frac{\frac{1}{I_n} \times \frac{V_n}{\sqrt{3}}}{\frac{1}{I_s} \times \frac{V_n}{\sqrt{3}}} = \frac{Z_b}{Z_s} = \frac{1}{Z_{spu}}$$

④ 电压調整率

$$VR\% = \frac{E_A - V_\phi}{V_\phi} \times 100\%$$

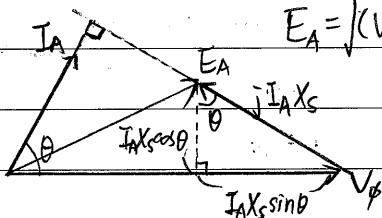
功因落後

$$E_A = \sqrt{(V_\phi + I_A X_s \sin \theta)^2 + (I_A X_s \cos \theta)^2}$$

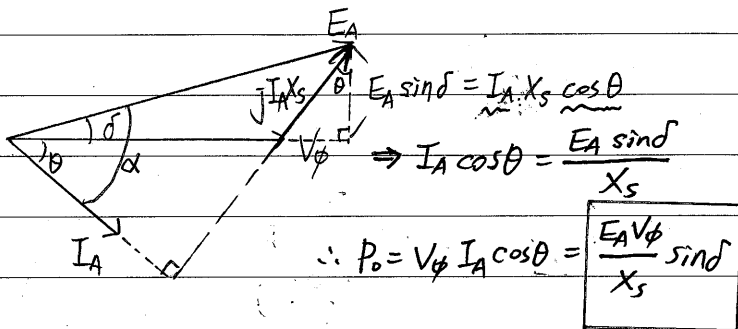
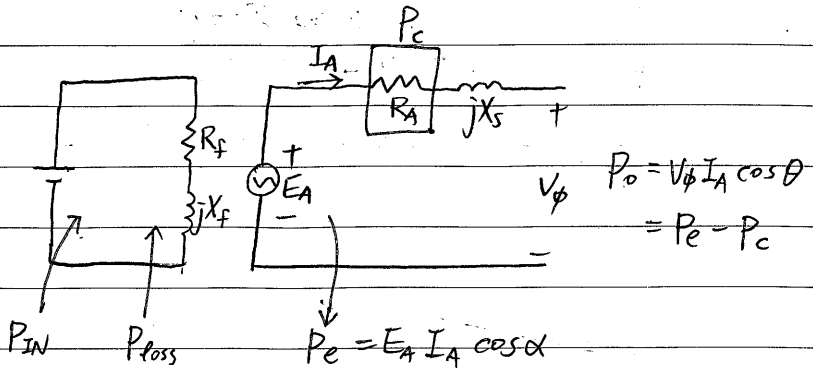


功因超前

$$E_A = \sqrt{(V_\phi - I_A X_s \sin \theta)^2 + (I_A X_s \cos \theta)^2}$$



⑤ 功率分佈 $\Rightarrow$ 每相等效电路



⑥ 並聯運用 $\Rightarrow$ 电压 $\Rightarrow V(t) = V_m \sin(2\pi f t + \theta)$

條件：① 感應电压大小相同

② " 波形 "

③ " 頻率 "

④ " 相位 "

⑤ " 相序 "

① 無角度

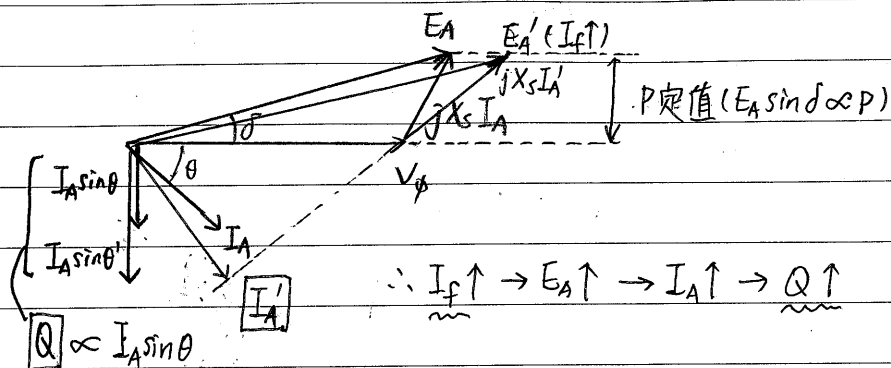
② 每相

③ $\frac{E_A V_\phi}{X_s}$ 最大

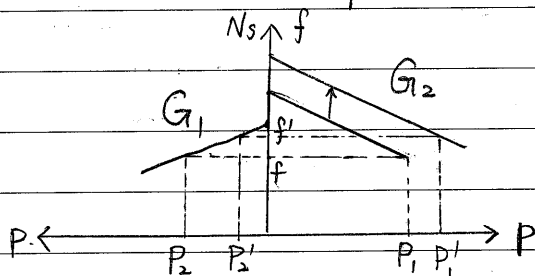
避免產生

內部環流

⑦ 負載分配

 $\Rightarrow$ $I_f \Rightarrow$ 虛功率 $N_s \Rightarrow$ 實功率
(f)**虛功率** $\Rightarrow I_f \propto Q$ [條件: V_ϕ, P 定值]**實功率** $\Rightarrow N_s(f) \propto P$

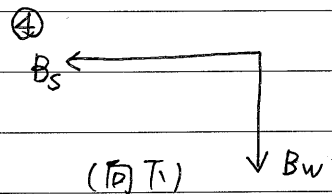
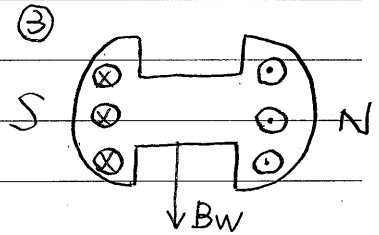
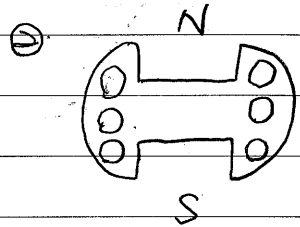
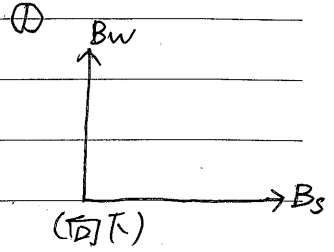
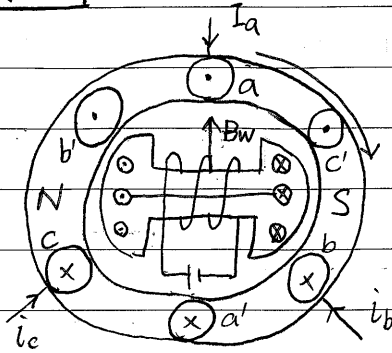
$$(N_s = \frac{120f}{P})$$

 $N_s \uparrow \rightarrow f \uparrow$

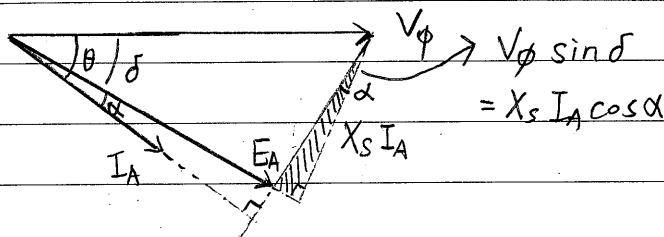
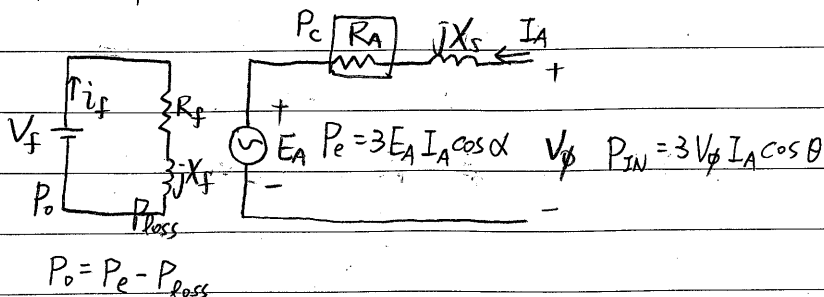
$$P_L = P_1 + P_2 = P_1' + P_2'$$

§ Ch4. 同步電動機 $\Rightarrow$ 無法自行啟動 $\Rightarrow$ 阻尼繞阻

① 原理



功率分佈 (每相等效电路):



不計 P_{loss} 時, $P_o = P_e$

$$P_o = E_A I_A \cos \alpha$$

(每相)

$$= E_A \frac{V_\phi \sin \delta}{X_s} =$$

$$\boxed{\frac{E_A V_\phi}{X_s} \sin \delta}$$

② 激磁特性

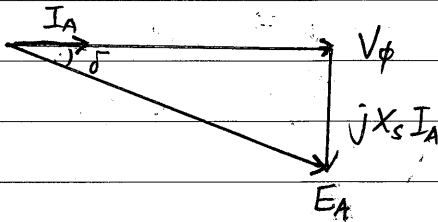
條件：端电压，轉矩為定值
(V_ϕ) (P)

目的：調整 I_A , $\cos \theta$

① 正常激磁

$$\left[\begin{array}{l} \cos \theta = 1 \\ I_A \text{ 最小} \end{array} \right.$$

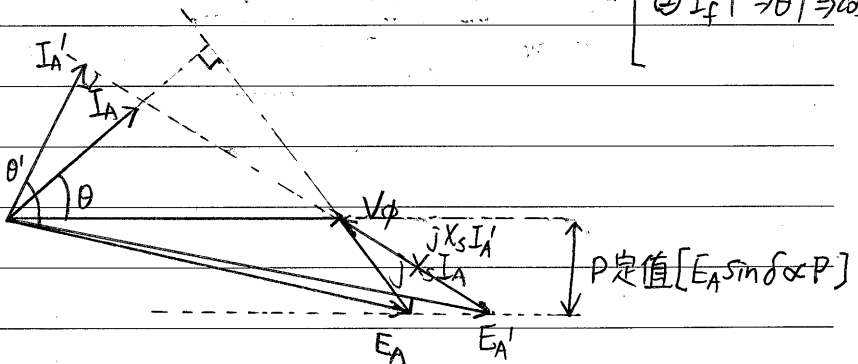
調整 I_f 使 V_ϕ 与 I_A 同相位



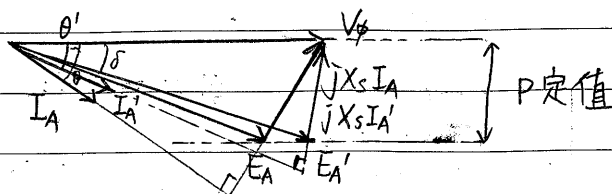
② 过激磁 ($I_f \uparrow \Rightarrow E_A \uparrow$)

$$\textcircled{1} I_f \uparrow \Rightarrow I_A \uparrow$$

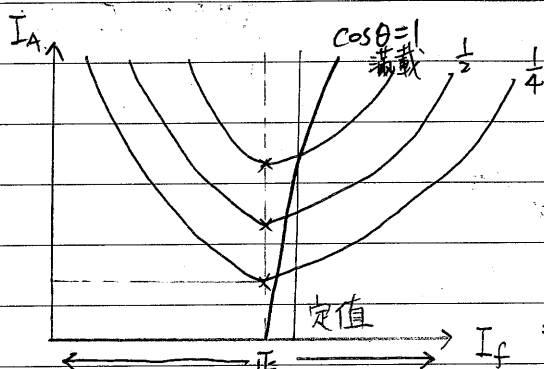
$$\textcircled{2} I_f \uparrow \Rightarrow \theta \uparrow \Rightarrow \cos \theta$$



③ 欠激磁 ($I_f \downarrow \Rightarrow E_A \downarrow$)



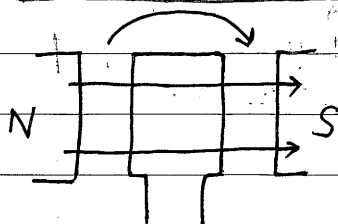
① $I_f \uparrow \Rightarrow I_A \downarrow$
 ② $I_f \uparrow \Rightarrow \theta \downarrow \Rightarrow \cos \theta \uparrow$



欠激磁 (落后功因) 正常激磁 (超前功因) 过激磁
 正交磁 去磁

I_f 定值, 增加负载
 $\Rightarrow$ 功率因数由超前 $\rightarrow$ 落后

§ Ch5. 直流機

① 產生感應電勢 E_{av} 

換向器

$$\phi(t) = \phi \cos \omega t$$

$$e = -N \frac{d\phi}{dt} = \boxed{\phi \omega} \sin \omega t$$

(N=1)

$$\therefore E_{av} = \frac{2V_m}{\pi} \times \frac{Z_a}{2} \times \frac{1}{a}$$

每匝平均電壓 每并路徑表之匝數

$$= \frac{2\phi \omega}{\pi} \times \frac{Z_a}{2} \times \frac{1}{a}$$

$$= \frac{2\phi 2\pi f}{\pi} \times \frac{Z_a}{2} \times \frac{1}{a}$$

$$= \frac{2\phi 2\pi \frac{Pn}{120}}{\pi} \times \frac{Z_a}{2} \times \frac{1}{a}$$

↑

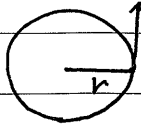
$$\frac{N_s P}{60} \times \frac{1}{2} = f$$

$$= \boxed{\frac{P Z_a}{60a}} \times \phi \cdot n$$

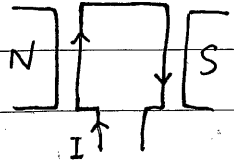
$$= K \phi n$$

② 產生轉矩 (T)

$$T = \boxed{F} \times r$$



$$F = \boxed{B} \ell \boxed{I} \text{ (單一導體)}$$

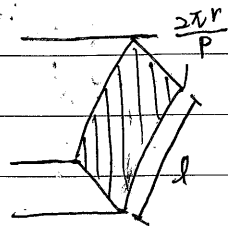


$$\therefore F = \frac{\phi}{A} \times l \times I \times Z_a$$

$$= \frac{\frac{\phi}{2\pi r}}{P} \times l \times \frac{I}{a} \times Z_a$$

$$= \frac{P\phi}{2\pi r} \times l \times \frac{I}{a} \times Z_a$$

$$= \frac{P\phi}{2\pi r} \times \frac{I}{a} \times Z_a$$



$$\therefore T = F \times r$$

$$= \frac{P\phi}{2\pi r} \times \frac{I}{a} \times Z_a \times r$$

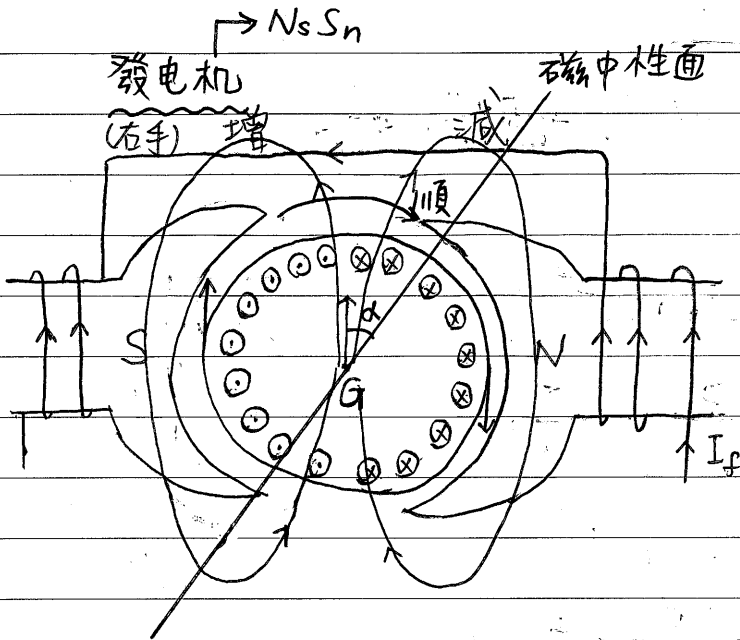
$$= \boxed{\frac{P Z_a}{2\pi a}} \times \phi \times I$$

$$= K \phi I$$

③ 电枢反应

主磁場

电枢磁場 → 減弱 → 改善电枢反应



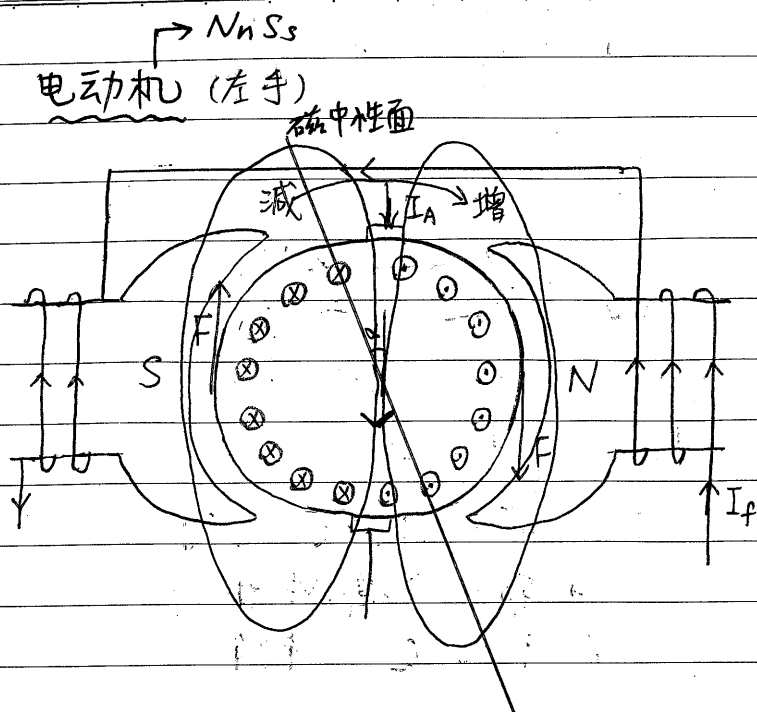
前極尖磁通減少

後極尖磁通增加

磁中性面 順 旋轉方向移动

电刷

"



前極尖磁通增加
後極尖磁通減少
磁中性面 逆 旋轉方向移動
電刷

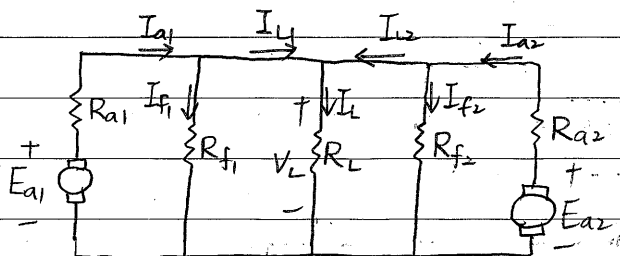
△ 補償繞阻

△ 中間極

並聯運用

分激式
積複激式

④ 分激式



條件：

① 端电压太小相同

② 端电压极性相同

③ $P_L = V_L I_L$ (V_L 定值)

$$\therefore P_L \propto I_L$$

容量與負載電流成正比

④ 外部特性曲線相同

負載分配：

$$P_L \propto I_L \Rightarrow \frac{P_{L1}}{P_{L2}} = \frac{I_{L1}}{I_{L2}}$$

$$\text{又 } E_A = V_L + I_a R_a \quad (E_A, V_L \text{ 定值})$$

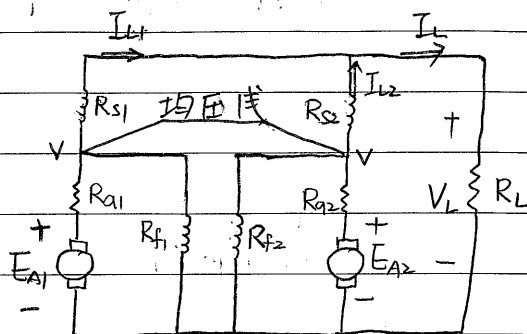
$$\therefore \frac{I_{a1}}{I_{a2}} = \frac{R_{a2}}{R_{a1}}$$

$$\Rightarrow \boxed{\frac{I_{L1}}{I_{L2}} = \frac{P_{L1}}{P_{L2}} = \frac{R_{a2}}{R_{a1}}}$$

R_a 已知 $\Rightarrow$ 解聯立, 求 I_{L1} 、 I_{L2}

$$\begin{cases} I_L = I_{L1} + I_{L2} \\ V_L = E_{A1} - I_{L1} R_{a1} = E_{A2} - I_{L2} R_{a2} \\ (I_a \doteq I_L) \end{cases}$$

⑤ 積複激式



條件: $\begin{bmatrix} ① \\ ② \\ ③ \\ ④ \end{bmatrix}$ 分激式相同

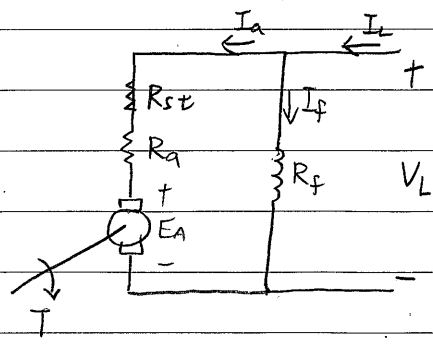
⑤ 裝設均壓式

⑥ $I_{L1} R_{s1} = I_{L2} R_{s2} \Rightarrow \boxed{\frac{I_{L1}}{I_{L2}} = \frac{R_{s2}}{R_{s1}}}$

負載分配:

$$\boxed{\frac{I_{L1}}{I_{L2}} = \frac{P_1}{P_2} = \frac{R_{s2}}{R_{s1}}}$$

⑥ 启动 $\Rightarrow$ $\left[\begin{array}{l} \text{降低启动电流} \rightarrow \text{串接电阻} \\ \text{增加启动转矩} \end{array} \right]$



$n=0 \Rightarrow E_A=0$

$I_{As} = \frac{V_L - E_A^0}{R_a}$

$R_{st} = \frac{V_L - E_A}{I_{as}} - R_a - R_s$

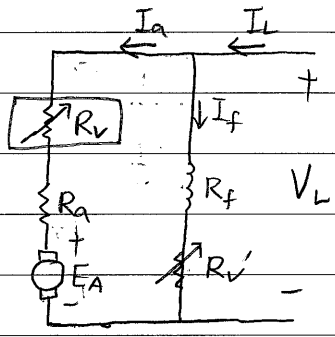
$\hookrightarrow$ 串激式

⑦ 速率控制

$E = K\phi n$

$\Rightarrow n = \frac{V_L - I_a R_a}{K\phi}$

① 电枢电阻控制法



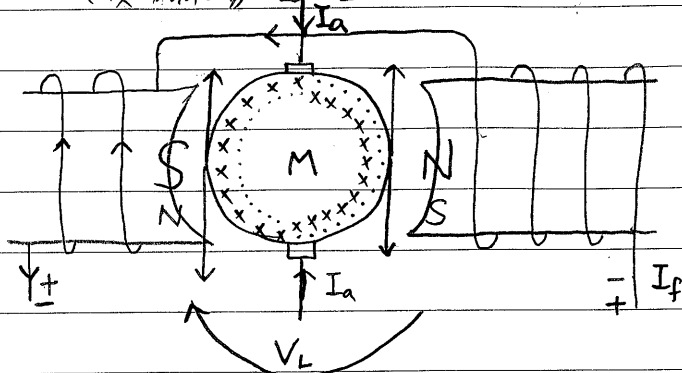
$R_v \uparrow \rightarrow E_A \downarrow \rightarrow n \downarrow$

$R_v' \uparrow \rightarrow I_f \downarrow \rightarrow \phi \downarrow \rightarrow n \uparrow$

⑧ 車云向控制

⇒ 佛萊銘 左手

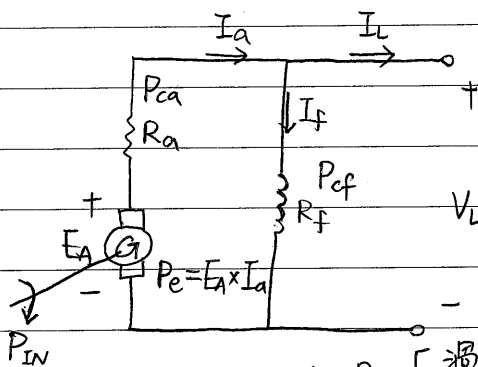
⇒ 改变电枢电流
改变磁場極性



順時針

⑨ 功率分配 ⇒ 看等效电路

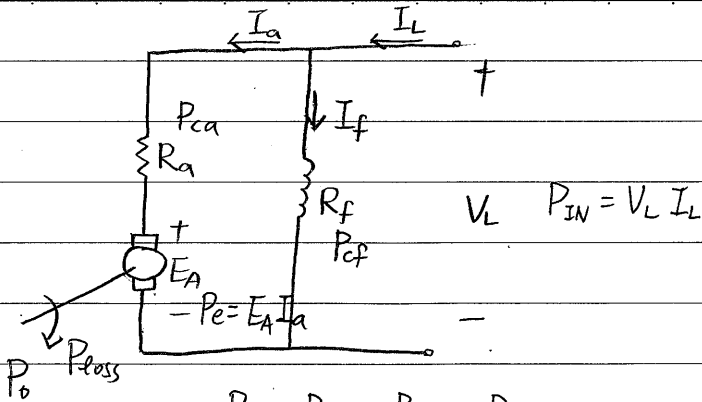
無載 ⇒ $I_a = I_f$ ($I_L = 0$)



$$P_o = P_e - P_{ca} - P_{cf}$$

$$= P_{IN} - P_{loss} - P_{ca} - P_{cf}$$

$P_{loss} \Rightarrow$ [鐵損] [渦流 $\propto n^2$
[機械損] [磁滯 $\propto n$
[旋轉損] [摩擦
[風阻]



$$P_e = P_{IN} - P_{ca} - P_{cf}$$

$$P_o = P_e - P_{loss}$$

無載 $\Rightarrow P_{loss} = P_e$